

POSE ESTIMATION USING STRUCTURED LIGHT AND HARMONIC SHAPE CONTEXTS

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Keywords: Bin-picking, rotational invariant features, surface mesh, time multiplexed binary stripes, CAD model

Abstract: One of the remaining obstacles to a widespread introduction of industrial robots is their inability to deal with 3D objects in a bin that are not precisely positioned, i.e., the bin-picking problem. In this work we address the general bin-picking problem where a CAD model of the object to be picked is available beforehand. Structured light, in the form of Time Multiplexed Binary Stripes, is used together with a calibrated camera to obtain 3D data of the objects in the bin. The 3D data is then segmented into points of interest and for each a regional feature vector is extracted. The features are the Harmonic Shape Contexts. These are characterized by being rotational invariant and can in general model any free-form object. The Harmonic Shape Contexts are extracted from the 3D scene data and matched against similar features found in the CAD model. This allows for a pose estimation of the objects in the bin. Tests show the method to be capable of pose estimating partial-occluded objects, however, the method is also found to be sensitive to the resolution in the structured light system and to noise in the data.

1 INTRODUCTION

One of the remaining obstacles to a widespread introduction of industrial robots is their inability to deal with 3D objects that are not precisely positioned, e.g., objects supplied in bins, see figure 1. The general problem of robots handling objects located in bins or containers is known as the bin-picking problem (Torras, 1992).

Due to multiple objects in multiple layers, occlusion causes severe problems for any automatic bin-picking system. However, two issues make the problem tractable, i) the fact that only one type of object is usually present in a bin, and ii) the fact that a CAD model of the object type in the bin is normally known beforehand.

The automated bin-picking problem has been addressed using various technologies and different methods. One approach is to first find a plane region in an object, isolating it from the rest of the objects using a vacuum gripper and then do the final pose estimation using some computer vision techniques. In (Berger et al., 2000) the plane regions are identified using a grid projector combined with a binocular stereo setup placed above the bin. In (Saldner, 2003)

a fringe placed in front of a video projector is used together with a high resolution camera.

A different approach is to match the CAD model directly with the objects in the bin. This can for example be carried out using the appearance (Balslev and Eriksen, 2002) or circular features (Moeslund and Kirkegaard, 2005). Alternatively, 3D data of the scene can be found¹ and matched directly with the CAD model, e.g., using a laser scanner (Schraft and Ledermann, 2003; Bougborbel et al., 2003), Active Depth From Defocus (Ghita and Whelan, 2003), or Structured Light (Salvi et al., 2004).

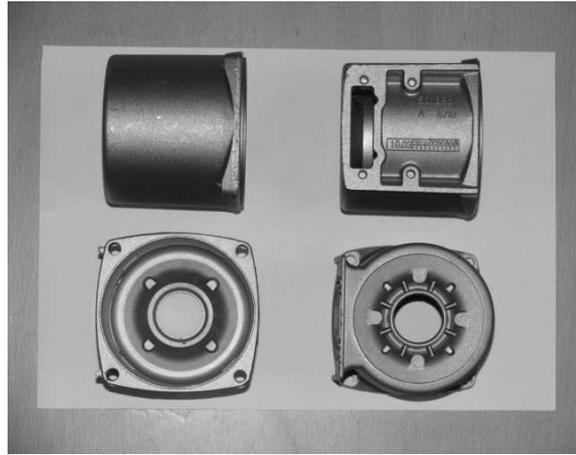
1.1 CONTENT OF THE PAPER

In this work we address the problem of automated bin-picking using structured light. The reason for using structured light is that it can support both the principle of finding plane regions in objects as well as finding the pose of an object directly in the bin. The problem is addressed generally, in the sense that nothing is assumed about the shape of the objects except that a CAD model is present. We use one particularly

¹See (Schwarte et al., 1999; Curless, 2000) for overviews of 3D imaging methods.



(a) A bin containing randomly organized stator housings.



(b) The stator housing object shown from four different viewpoints on a piece of A4 paper for reference.

Figure 1: Depiction of the stator housings.

object type to validate our approach. This is a stator housing object, see figure 1, produced at Grundfos, one of the world’s leading pump manufacturers (www.grundfos.com, 2005).

Since the detection of plane regions has been addressed thoroughly in the past we shall in this paper focus on finding invariant features for non-plane regions. The paper is structured as follows. In section 2 it is described how the 3D surface of the objects in the bin are reconstructed. In section 3 it is described how the invariant features are defined and extracted. In section 4 the matching between the CAD model and bin data is described. In section 5 the results are presented and finally section 6 concludes the work.

2 RECONSTRUCTING THE 3D SURFACE

The structured light system is based on a standard LCD projector and a single JAI monochrome CCD camera. The encoding scheme used is *Time Multiplexed Binary Stripes* (Posdamer and Altschuler, 1982).

The basic principle is to project a series of patterns onto the scene encoding each scene point by a series of illumination values. The utilized patterns are binary gray encoded multi stripe patterns, where the binary property refers to the use of two different illumination values (no and full) (Valkenburg and McIvor, 1998). More specifically the gray codes ensure, that adjacent codewords only differ by a single bit, which in turn ensures that transitions between black and white stripes do not occur at the same po-

sition in all patterns concurrently. This principle is illustrated in figure 2.

We use 8 bits, i.e., encoding 256 stripes with the LSB pattern stripes being 4 pixels wide, see figure 3. Apart from the eight gray encoded patterns (I_0, \dots, I_7), two additional images are obtained of the scene, i.e., a full-illumination (I_H) and a zero-illumination image (I_L). These are used in equation 1 to compensate for ambient light and a possibly non-constant albedo of the objects in the scene. By subtracting I_L from the pattern images, they are compensated for ambient light effects. The denominator term is proportional to the object albedo, thereby creating an albedo normalized image, see figure 3.

$$J_k = \frac{I_k - I_L}{I_H - I_L} \quad (1)$$

2.1 REPRESENTING THE SURFACE

After thresholding the albedo normalized images we have a series of binary images B_0, \dots, B_7 , which in turn provide the projector coordinate encoding of each pixel, see figure 3. Combining this with a calibration between the projector and the camera yields a number of 3D points representing the scene (Kirkegaard, 2005). These points are subjected to a Tessellation process, which yields a simple triangular mesh representing the surfaces in the scene. The basic assumption enabling the creation of the mesh is, that world points originating from neighboring pixels in the stripe image are also neighbors in the scene, i.e., these are connected.



Figure 2: The principle behind the gray coded binary representation. Each row indicates a given bit with the least significant bits placed in the top row. Each column indicates all the bits of one codeword.

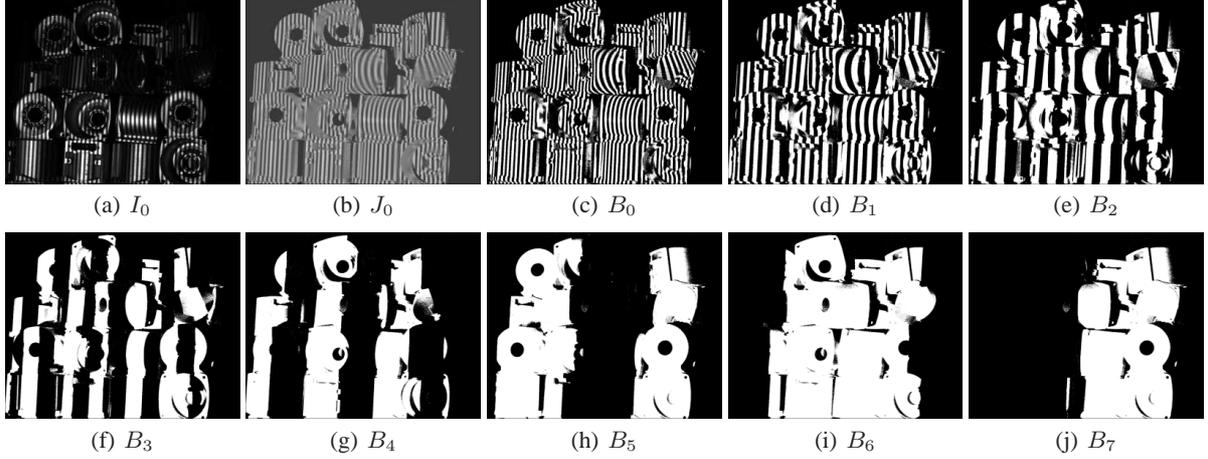


Figure 3: The principle of Time Multiplexed Binary Stripes when using a resolution of 8 bits.

Basically the reconstructed surface is a piecewise-linear surface consisting of triangles. These triangles will not be a perfect representation primarily due to the presence of noise in the reconstruction process, e.g., from the quantization due to the finite number of stripes and the crude approximation of object albedo. Therefore a smoothing of the rectangles is preformed based on the weight of the three vertices in a triangle.

The weight of each vertex, i.e., the weight of each reconstructed 3D point, can be found from equation 1. The value of the pixels in the J_k images can give an indication of the quality or *fidelity* of the actual pixel. To give a quantitative measure of the pixel *fidelity* it is assumed that the normalized intensity images J_k are contaminated by zero-mean Gaussian noise $\xi(x, y)$ with variance σ^2 . Given $J_k(x, y) > 0.5$ the pixel fidelity can be expressed as (Bronstein et al., 2003):

$$\begin{aligned} F_k(x, y) &= P \{J_k(x, y) + \xi(x, y) > 0.5\} \Leftrightarrow \\ F_k(x, y) &= \Phi \left(\frac{0.5 - J_k(x, y)}{\sigma} \right) \end{aligned} \quad (2)$$

where $\Phi(\cdot)$ denotes the cumulative distribution function for the normal distribution. Similar for $J_k(x, y) < 0.5$ we have:

$$\begin{aligned} F_k(x, y) &= P \{J_k(x, y) + \xi(x, y) < 0.5\} \Leftrightarrow \\ F_k(x, y) &= \Phi \left(\frac{J_k(x, y) - 0.5}{\sigma} \right) \end{aligned} \quad (3)$$

Errors in the most significant bit pattern effects the stripe image more severe than errors in the less signif-

icant patterns. Therefore it is necessary to weigh the fidelity by stripe significance. The pixel fidelity is defined by (Bronstein et al., 2003) as equation 4 where the term 2^{-k} is the stripe significance weighing. The variance σ^2 has been set to unity.

$$\begin{aligned} F(x, y) &= \sum_{k=0}^{N-1} 2^{-k} F_k(x, y) \Leftrightarrow \\ F(x, y) &= \sum_{k=0}^{N-1} 2^{-k} \Phi \left(\left| \frac{0.5 - J_k(x, y)}{\sigma} \right| \right) \end{aligned} \quad (4)$$

3 EXTRACTING FEATURES

The 3D mesh (and CAD model) provides a vast amount of different 3D positions from where features can be calculated. However, some locations are better than others. For example, features on a large smooth surface might not be the best choice since these by nature will result in ambiguities in the matching process. Therefore we do a segmentation of the mesh (and CAD model) in order to find positions where the ambiguity is low.

The general idea is to find positions where the curvature of the mesh changes (Trucco and Verri, 1998) and then calculate invariant features at these positions. The change of curvature is found by evaluating the change in the signs of the Principal Curvatures (Kirkegaard, 2005).

3.1 SHAPE CONTEXTS

Before a matching between the segmented points and the CAD model can take place a number of features are to be extracted. We aim at a regional feature which characterizes the surface in a small finite region around each point of interest. A regional feature is a compromise between global and local surface features combining the noise robustness of the former with the occlusion robustness of the latter. Concretely we apply the Harmonic Shape Contexts as features. Since these are a generalization of the Shape Context features we start by explaining these.

Shape contexts are regional 3D shape features based on an oriented set of 3D points together with a multi-dimensional histogram. The support region for a shape context is a sphere centered at the point of interest with the sphere's north pole vector aligned with the normal vector of the mesh in this point (Frome et al., 2004), see figure 4.

The support region is divided linearly in the azimuthal (east-west) and in the colatitudinal (north-south) directions of the sphere, while the support sphere is divided logarithmically in the radial dimension. The number of cells are S , T , and U for the azimuthal, colatitudinal, and radial dimensions, respectively. Altogether this division results in $S \times T \times U$ cells representing the support sphere around the point of interest. A single cell in the sphere corresponds to one element in a feature vector for the point of interest. The support region for the shape contexts is illustrated in figure 4.

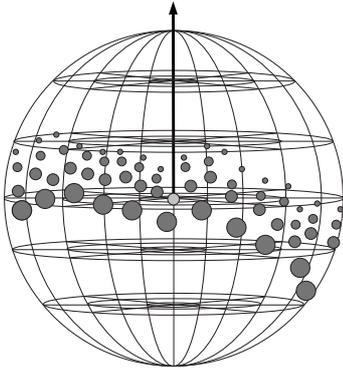


Figure 4: The spherical support region of the shape contexts.

A given cell accumulates a weighted count for each neighborhood point whose spherical coordinates fall within the ranges of the cell. The actual contribution (i.e., the weighing) to the cell count is given by the function $w(\cdot)$ (equation 5) for a given point \mathbf{p}_i .

$$w(\mathbf{p}_i) = \frac{1}{\rho_i \sqrt[3]{V}} \quad (5)$$

The element ρ_i in equation 5 is the local point density around the cell, while the function V denotes the volume of the cell. The normalization by the point density accounts for variations in sampling density, i.e., the same surface point may have varying numbers of neighborhood points given different image acquisition viewpoints. The normalization by the volume counteracts the effects of varying cell sizes. (Frome et al., 2004) found empirically, that normalizing by the cubic root of the cell volume retains discriminative power while leaving the feature robust to noise caused by points crossing cell boundaries.

Different shape contexts cannot be compared by simple correlation due to the shape contexts not being rotationally invariant, i.e., there exist a degree of freedom in the choice of orientation of the azimuthal direction. The shape contexts can however be made rotationally invariant by enhancing it by use of spherical harmonics - The Harmonic Shape Contexts (Kazhdan et al., 2003).

3.2 HARMONIC SHAPE CONTEXTS

Any given spherical function, i.e., a function $f(\theta, \phi)$ defined on the surface of a sphere parameterized by the colatitudinal and azimuthal variables θ and ϕ , can be decomposed into a weighted sum of spherical harmonics as given by equation 6.

$$f(\theta, \phi) = \sum_{l=0}^{\infty} \sum_{m=-l}^l A_l^m Y_l^m(\theta, \phi) \quad (6)$$

The terms A_l^m are the weighing coefficients of *degree* m and *order* l , while the complex functions $Y_l^m(\cdot)$ are the actual spherical harmonic functions of *degree* m and *order* l . Figure 5 depicts the principle of expressing a given spherical function by an infinite sum of weighted spherical harmonic basis functions.

The following states the key advantages of the mathematical transform based on the family of orthogonal basis functions in the form of spherical harmonics. A more thorough description can be found in (Kirkegaard, 2005).

The complex function $Y_l^m(\cdot)$ is given by equation 7, where $j = \sqrt{-1}$.

$$Y_l^m(\theta, \phi) = K_l^m P_l^{|m|}(\cos \theta) e^{jm\phi} \quad (7)$$

The term K_l^m is a normalization constant, while the function $P_l^{|m|}(\cdot)$ is the *associated Legendre Polynomial*. The key feature to note from equation 7 is the encoding of the azimuthal variable ϕ . The azimuthal

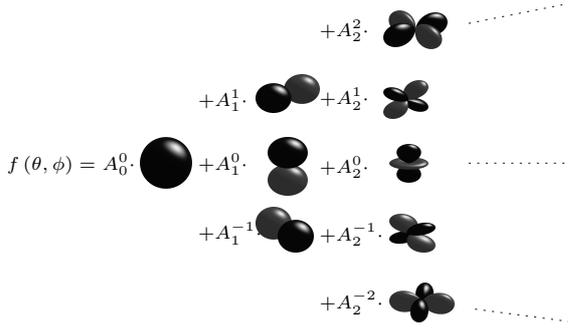


Figure 5: A spherical function expressed as a linear combination of spherical harmonic basis functions. Black indicates positive values and gray negative values.

variable solely inflects the *phase* of the spherical harmonic function and has no effect on the *magnitude*. This effectively means that $\|A_l^m\|$, i.e., the norm of the decomposition coefficients of equation 6 are invariant to parameterization in the variable ϕ .

The rotationally invariant property of the spherical harmonic transformation makes it suitable for use in encoding the shape context representation enabling a more efficient comparison. For a given spherical shell corresponding to all cells in a given radial division u , a function f_u is defined given by equation 8.

$$f_u(\theta, \phi) = SC(s, t, u) \quad (8)$$

where $SC(s, t, u)$ means the shape context representation where s (azimuthal direction), t (colatitudinal direction), and u (radial division) are used to index a particular cell.

The primary idea in the encoding process, is then to determine the coefficients A_l^m for each of the functions f_u for $u \in [0; U - 1]$. Based on the function in each spherical shell, a function $SH(\cdot)$ can be defined as given by equation 9.

$$SH(l, m, u) = \|(A_l^m)_{f_u}\| \quad (9)$$

where $(A_l^m)_{f_u}$ denotes the spherical harmonic coefficient of order l and degree m determined from decomposition of the spherical function f_u . The function $SH(\cdot)$ is then an invariant regional surface feature based on the principle of the shape contexts.

The actual determination of the spherical harmonic coefficients is based on an inverse summation as given by equation 10, where N is the number of samples ($S \times T$). The normalization constant $4\pi/N$ originates from the fact, that equation 10 is a discretization of a continuous double integral in spherical coordinates, i.e., $4\pi/N$ is the surface area of each sample on the unit sphere.

$$(A_l^m)_{f_u} = \frac{4\pi}{N} \sum_{\phi=0}^{2\pi} \sum_{\theta=0}^{\pi} f_u(\theta, \phi) Y_l^m(\theta, \phi) \quad (10)$$

In a practical application it is not necessary (or possible, as there are infinitely many) to keep all coefficient A_l^m . Contrary, it is assumed the functions f_u are band-limited why it is only necessary to keep coefficient up to some bandwidth $l = B$.

The band-limit assumption effectively means, that each spherical shell is decomposed into $(B + 1)^2$ coefficients (i.e., the number of terms in the summation $\sum_{l=0}^B \sum_{m=-l}^l$ in equation 6). By using the fact, that $\|A_l^m\| = \|A_l^{-m}\|$ and only saving coefficients for $m \geq 0$, the number of describing coefficients for each spherical shell is reduced to $(B + 1)(B + 2)/2$ coefficients (i.e., the number of terms in the summation $\sum_{l=0}^B \sum_{m=0}^l$). Given the U different spherical shells, the final dimensionality of the feature vector becomes

$$D = U(B + 1)(B + 2)/2 \quad (11)$$

The actual comparison between two harmonic shape contexts is done by the normalized correlation between two D dimensional feature vectors. A correlation factor close to unity resembles a good match, while a correlation factor close to zero represent a very poor match.

3.3 TUNING THE HARMONIC SHAPE CONTEXTS

The number of azimuthal and colatitudinal divisions have no influence on the dimensionality of the harmonic shape context feature vector. However, the chosen divisions have influence on both the discriminative power as well as the matching efficiency. Furthermore, the number of angular divisions inflect the required computation when determining spherical harmonic coefficients based on the shape contexts (equation 10). As a trade-off between discriminative power and encoding time complexity **16** colatitudinal divisions and **32** azimuthal divisions are used. For the radial division we empirically found that **10** divisions spanned logarithmically between **5** and **25mm** is the best trade off. Finally the bandwidth parameter B is set to **15** and the final number of coefficients in each feature vector can be calculated from equation 11

$$10(15 + 1)(15 + 2)/2 = 1360 \quad (12)$$

To get a better understanding of the harmonic shape contexts we illustrate some of the coefficients in the feature vectors for three points on a reconstructed mesh 7. The outer shell of the shape contexts for the three points are shown as the first row in figure 7. The

three figures depict the count for each of 32×16 bins contained in the shell. The first colatitudinal bin corresponds to the bin around the north pole, while the last bin corresponds to the south pole bin. The three corresponding harmonic shape contexts for the three points are shown in the second row. The figures depict the spherical harmonic coefficients for each of the 10 shells together with the 36 first coefficients out of the total of 136 in each shell.

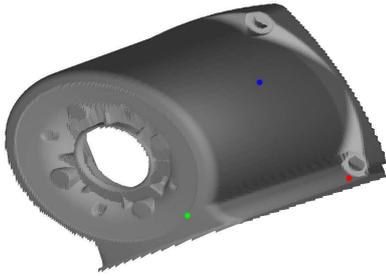


Figure 6: Object mesh with three color-marked points.

4 MATCHING

The primary purpose of extracting harmonic shape contexts from the scene and CAD model is to perform a matching. Due to the rotational and translational invariance of the harmonic shape context, a feature vector extracted from the CAD model and the scene at positions originating from the same stator housing object point should correlate well. Since the objects in the scene are likely to be partial (self)occluded we divide the CAD model into 64 sub-models seen from different points of view and match each of these with the extracted data.

The quality of a match cannot be judge solely by one normalized correlation factor, i.e., it is necessary to consider more matches at a time. This is formulated as a graph search problem and solved using simulated annealing (Kirkegaard, 2005).

After having found a number of matches we are left with a number of corresponding 3D points from the scene and CAD model. We now minimize an error function in order to find the rigid transformation between the model and scene, i.e., the pose of the object in the scene (Kirkegaard, 2005).

5 RESULTS

The primary evaluations performed on the method are based on synthetic data. This is done to be able to

quantitatively judge the results of the method. We first evaluate the method’s ability to handle occlusion, then noise and finally the resolution of the structured light system.

The CAD model is used to create the scene mesh by first using a simulated structured light system (using ray-tracing) and then doing a tessellation of the reconstructed 3D points (Kirkegaard, 2005). See figure 6 and 8 for examples.

A scene is constructed containing 12 randomly rotated, translated and partial occluded stator housings, see figure 8. The feature extraction and matching methods are applied and the results are visually inspected by transforming the models into the scene using the estimated pose parameters along with comparing the simulated and estimated pose parameters.

Six of the stator housings were pose estimated correctly down to five degrees of freedom, i.e., the “cylinder cup” where pose estimated correctly but without the remaining cylinder axis rotation, see figure 8. Two of the stator housings were pose estimated correctly with all six degrees of freedom. The primary reason for the many five degree of freedom results is due to the many symmetries contained in a stator housing object, i.e., it is only the particular terminal box of the stator housing object that enables the complete six degree of freedom pose estimation.

In table 1 we list the normalized frequency of correct pose estimations as a function of the level of random noise. The data is calculated by simulating a stator housing in 120 different configurations for each of the different noise levels. The random noise is added directly to the reconstructed 3D points and a correct pose estimation is defined to be when the $L2$ norm between the simulated and estimated rigid transformations is below 0.1 for both the rotation matrices and the translation vectors.

Table 1: Normalized frequency of correct pose estimations as a function of the level of simulated random noise [mm].

Noise	0.05	0.1	0.15	0.2	0.25	0.3
Pose	0.98	0.97	0.85	0.57	0.29	0.09

In table 2 we list the normalized frequency of correct pose estimations as a function of the resolution in the structured light system. The latter refers to the number of bits used to code the position of each pixel in the stripes. The same test setup as above is used.

Table 2: Normalized frequency of correct pose estimations as a function of the resolution in the structured light system [bit].

Res.	10	12	14	16	18	20
Pose	0.24	0.97	0.98	0.98	0.99	1.0

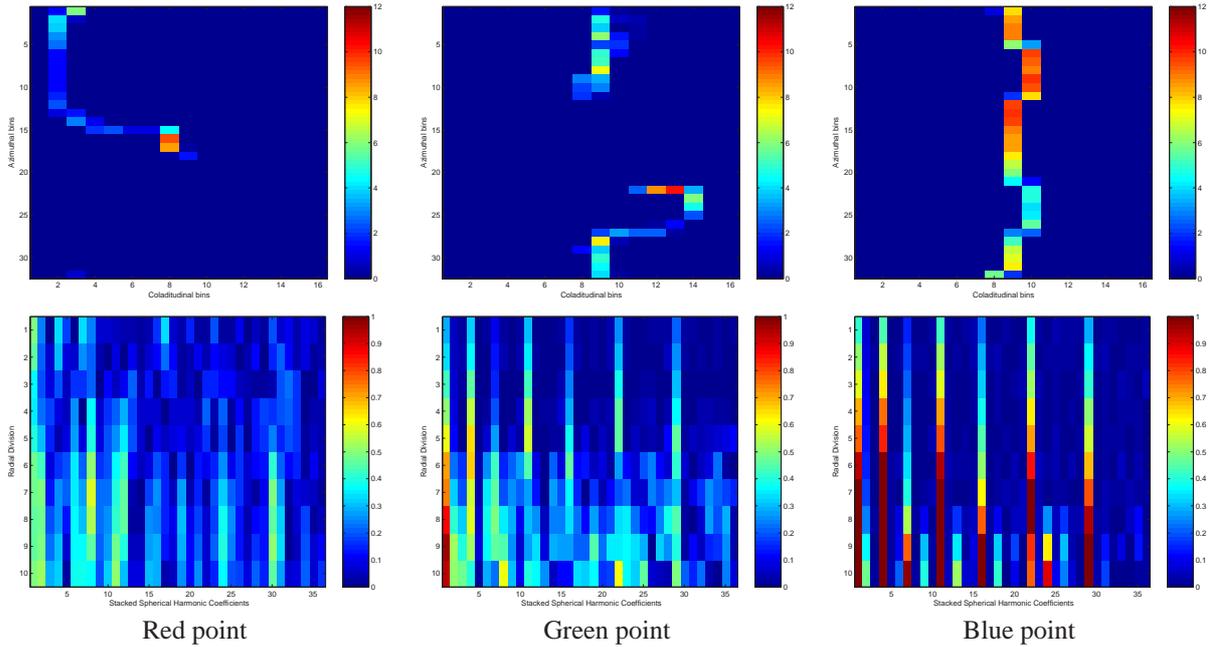


Figure 7: Illustrates shape contexts (first row) and harmonic shape contexts (second row) for the red, green, and blue points on the object mesh, respectively. Note that only the outer shell is visualized for the shape context and only the first 36 coefficients for the harmonic shape context.

6 DISCUSSION

We have in this work addressed the general bin-picking problem where a CAD model of the object to be picked from the bin is available beforehand.

The performed tests showed that the proposed method is capable of pose estimating 8 objects in a scene containing 12 randomly organized and thereby occluding stator housings for the case of simulated noise free meshes. Even though this is only $2/3$ of the objects it is still considered a success. Firstly because only one object is required to be pose estimated correct at a time (the scene will change after the robot has picked one object), and secondly because they are pose estimated very accuracy even in the presence of occlusion.

In some cases only five out of the six degrees of freedom were correctly estimated. This is a common problem in many bin-picking applications due to self-symmetry but can be solve by using a two-step solution as mentioned in the Introduction, i.e., first isolating one object and picking it (based on the five estimated pose parameters) and *then* pose estimating it using standard vision techniques.

When adding noise to the data table 1 showed that the performance decreases. This is mainly due to the fact that the harmonic shape contexts are depended on the direction of the normal vector. To some degree

this problem can be handled by tuning the number of bins to the noise-level. Alternatively a better smoothing mechanism is required.

From table 2 we can see that the resolution has a high impact on the performance. Therefore a high number of bits should be used, which again means that the camera has to be placed closed to the objects (allowing only a few objects to be present within the field of view) or the resolution of the projector and the camera has to be very high. The concrete setup in this work only allowed a resolution of eight bits, which turned out to be too low for the system to operate reliably. This result is in total agreement with table 2 where resolutions below 12 bits produce poor results.

In conclusion it can be stated that using harmonic shape contexts is a solid approach due to the fact that they can model any rigid object without assuming anything about the shape of the object *and* can handle partially occluded objects. This is not the case with the traditional approaches where one assumes simple shapes, e.g., planes or ellipses, to be present. In fact, the harmonic shape contexts can model any free-form object, but works best when an object contains surfaces with different curvatures. Therefore it seems naturally that future *general* bin-picking approaches should combine the harmonic shape contexts with approaches using more global features since these two approaches compliment each other.

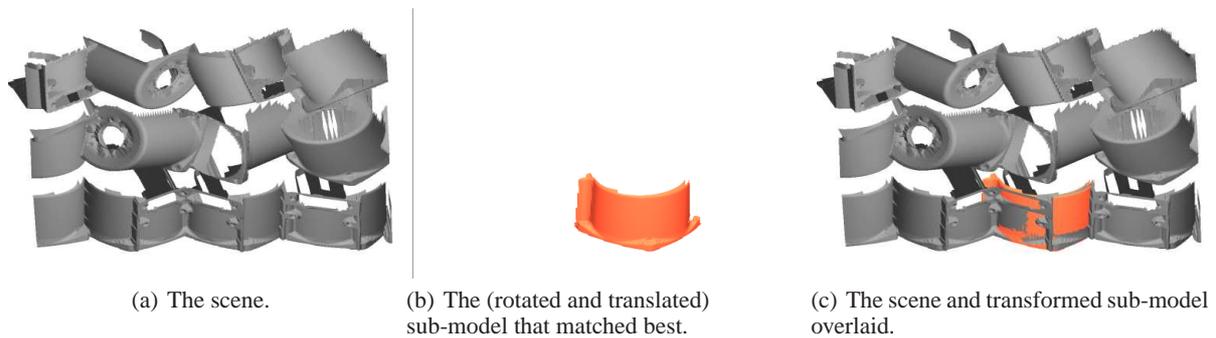


Figure 8: Depiction of a correct 5 degree of freedom pose estimation.

REFERENCES

- Balslev, I. and Eriksen, R. D. (2002). From belt picking to bin picking. *Proceedings of SPIE - The International Society for Optical Engineering*, 4902:616–623.
- Berger, M., Bachler, G., and Scherer, S. (2000). Vision Guided Bin Picking and Mounting in a Flexible Assembly Cell. In *Proceedings of the 13th International Conference on Industrial & Engineering Applications of Artificial Intelligence & Expert Systems, IEA/AIE2000*, pages 109–118, New Orleans, Louisiana, USA.
- Boughorbel, F., Zhang, Y., Kang, S., Chidambaram, U., Abidi, B., Koschan, A., and Abidi, M. (2003). Laser ranging and video imaging for bin picking. *Assembly Automation*, 23(1):53–59.
- Bronstein, A. M., Bronstein, M. M., Gordon, E., and Kimmel, R. (2003). High-resolution structured light range scanner with automatic calibration. Technical report, Technion - Israel Institute of Technology.
- Curless, B. (2000). Overview of active vision technologies. 3D Photography - Course Notes ACM Siggraph '00.
- Frome, A., Huber, D., Kolluri, R., Bulow, T., and Malik, J. (2004). Recognizing objects in range data using regional point descriptors. In *European Conference on Computer Vision (ECCV)*, pages 224–237, Prague, Czech Republic.
- Ghita, O. and Whelan, P. F. (2003). A bin picking system based on depth from defocus. *Machine Vision and Applications*, 13(4):234–244.
- Kazhdan, M., Funkhouser, T., and Rusinkiewicz, S. (2003). Rotation invariant spherical harmonic representation of 3d shape descriptors. In *SGP '03: Proceedings of the 2003 Eurographics/ACM SIGGRAPH symposium on Geometry processing*, pages 156–164, Sardinia, Italy.
- Kirkegaard, J. (2005). Pose Estimation of Randomly Organized Stator Housings using Structured Light and Harmonic Shape Contexts. Master's thesis, Lab. of Computer Vision and Media Technology, Aalborg University, Denmark.
- Moeslund, T. B. and Kirkegaard, J. (2005). Pose estimation of randomly organised stator housings with circular features. In *Scandinavian Conference on Image Analysis*, Joensuu, Finland.
- Posdamer, J. L. and Altschuler, M. D. (1982). Surface measurement by space-encoded projected beam systems. *Computer Graphics and Image Processing*, 18(1):1–17.
- Saldner, H. (2003). Palletpicker-3d, the solution for picking of randomly placed parts. *Assembly Automation*, 23(1):29–31.
- Salvi, J., Pags, J., and Battle, J. (2004). Pattern codification strategies in structured light systems. *Pattern Recognition*, 37(4):827–849.
- Schraft, R. D. and Ledermann, T. (2003). Intelligent picking of chaotically stored objects. *Assembly Automation*, 23(1):38–42.
- Schwarte, R., Heinol, H., Buxbaum, B., Ringbeck, T., Xu, Z., and Hartmann, K. (1999). *Principles of Three-Dimensional Imaging Techniques in "Handbook of Computer Vision and Applications"*, volume 1. The Academic Press, first edition.
- Torras, C. (1992). *Computer Vision - Theory and Industrial Applications*. Springer-Verlag, first edition.
- Trucco, E. and Verri, A. (1998). *Introductory Techniques for 3D Computer Vision*. Prentice Hall, first edition.
- Valkenburg, R. J. and McIvor, A. M. (1998). Accurate 3d measurement using a structured light system. *Image and Vision Computing*, 16(2):99–110.
- www.grundfos.com (2005).